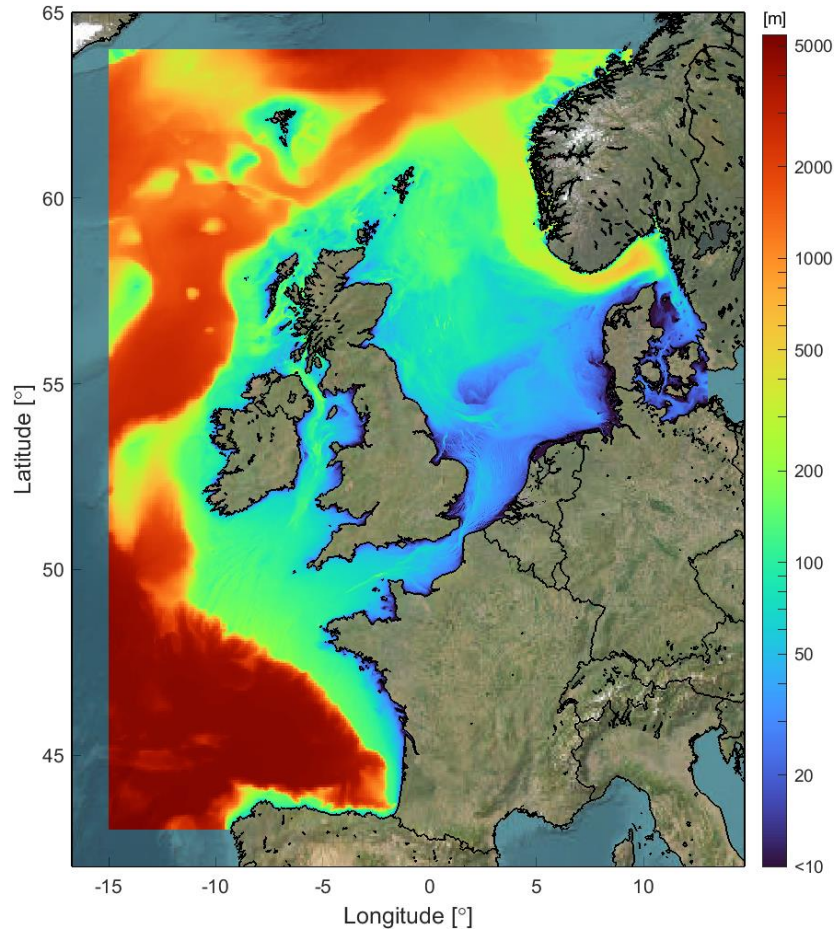


A bias-kalman-filter for operational storm-surge forecasting

Martin Verlaan, Tammo Zijlker,
Firmijn Zijl, Julius Sumihar

Deltares

Dutch Continental Shelf Model Delft3D-Flexible Mesh



Shallow-water tide-surge model

$$\frac{\partial h}{\partial t} + \nabla \cdot (H u) = 0$$

$$\frac{\partial u}{\partial t} + \frac{1}{H} (\nabla \cdot (H u u) - u \nabla \cdot (H u)) + f \times u$$

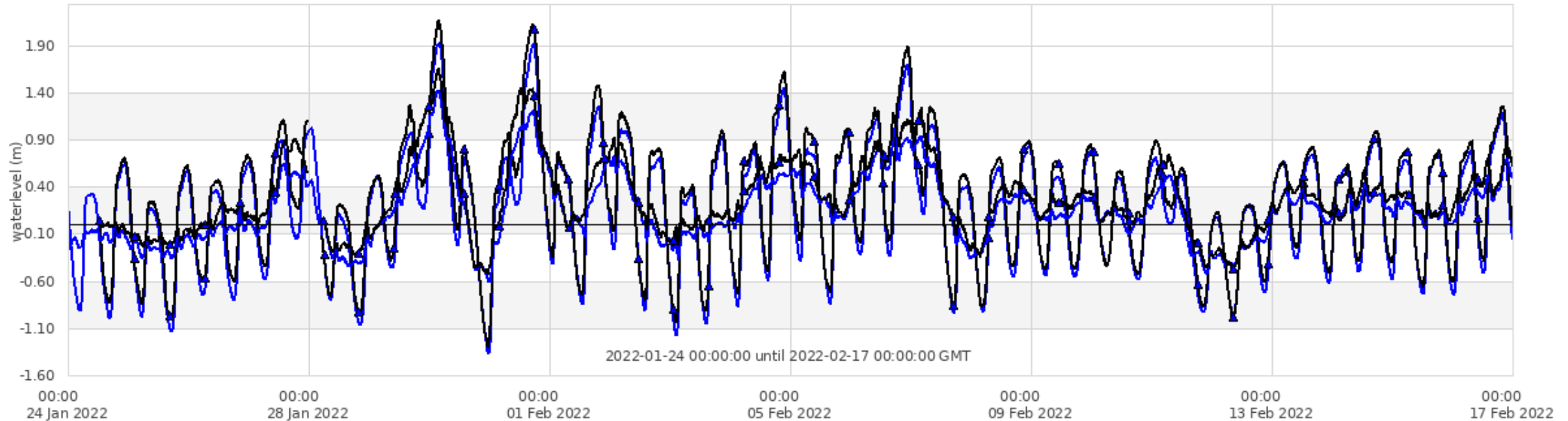
$$= -g \nabla \cdot (h - h_{\text{tide}}) - \frac{\nabla P_{\text{atm}}}{\rho} + \frac{\tau_{\text{atm}}}{\rho H}$$

Forcing:

- Tide
- Air-pressure and wind

Bias in operational storm-surge forecasts in 2022

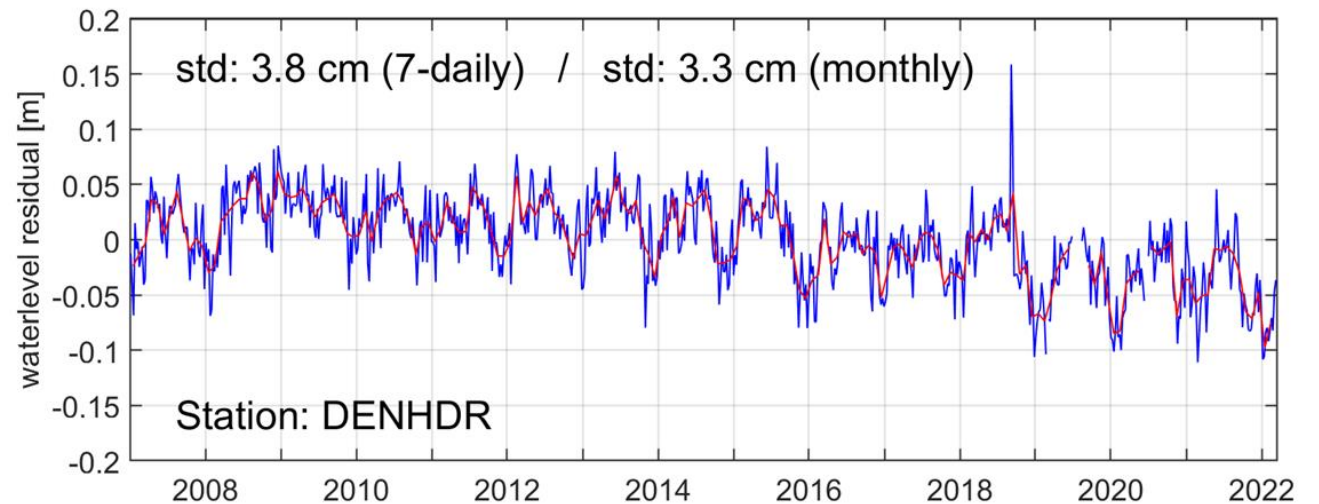
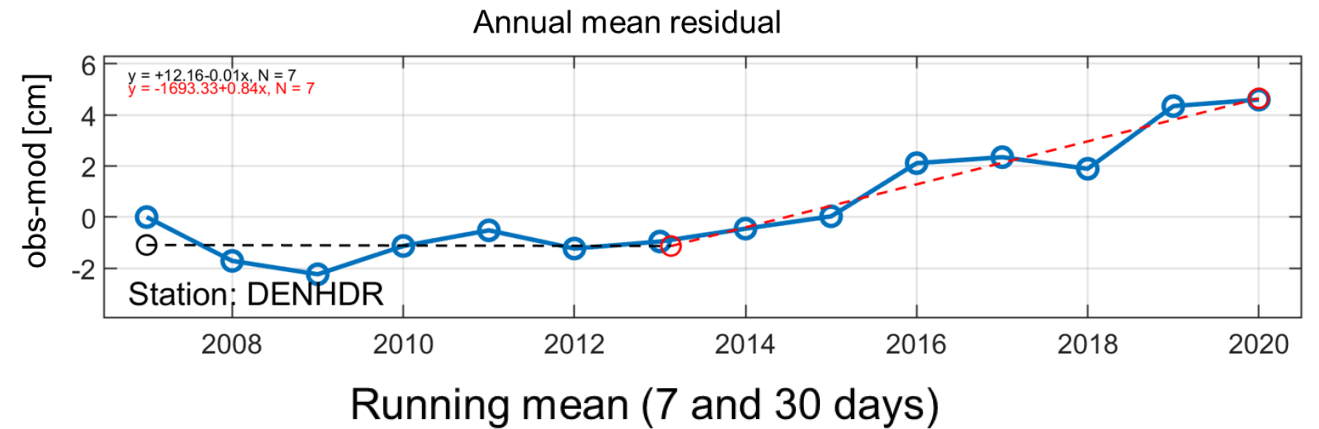
Den Helder



Model
Measurement

Possible causes


- Vertical referencing
 - Local subsidence / tide gauge benchmark
 - Issues in national vertical reference systems
 - Connection between countries
- Uncertainty in boundary conditions
 - Sea level rise
 - Seasonal variations
 - Long period ocean variations
- Model physics
 - 3D effects (density, temperature, salinity)



Ensemble Kalman filter – add ‘bias-force’ to model

EnKF

Time update

$$\begin{aligned}\xi_{k+1}^f(i) &= \mathbf{M}(\xi_k^a(i)) \\ \hat{\mathbf{x}}_k^f &= \frac{1}{N} \sum_{i=1}^N \xi_k(i) \\ \mathbf{P}_k^f &= \frac{1}{N-1} \sum_{i=1}^N (\xi_k^f(i) - \hat{\mathbf{x}}_k^f)(\xi_k^f(i) - \hat{\mathbf{x}}_k^f)'\end{aligned}$$


Measurement update

$$\begin{aligned}\mathbf{K}_k &= \mathbf{P}_k^f \mathbf{H}' [\mathbf{H} \mathbf{P}_k^f \mathbf{H}' + \mathbf{R}]^{-1} \\ \xi_k^a(i) &= \xi_k^f(i) + \mathbf{K}_k (\mathbf{z}_k - \mathbf{H} \xi_k^f(i) - \mathbf{v}_k(i))\end{aligned}$$

Model

Shallow water equations:

$$\begin{aligned}\frac{\partial h}{\partial t} + \nabla \cdot (H u) &= 0 \\ \frac{\partial u}{\partial t} + \frac{1}{H} (\nabla \cdot (H u u) - u \nabla \cdot (H u)) + f \times u \\ &= -g \nabla \cdot (h - h_{\text{tide}} - h_{\text{bias}}) - \frac{\nabla p_{\text{atm}}}{\rho} + \frac{\tau_{\text{atm}}}{\rho H}\end{aligned}$$

$$\mathbf{x} = \begin{bmatrix} h \\ u \\ h_{\text{bias}} \end{bmatrix}$$

Add term in pressure gradient, that will be balanced by sea-level if changes are slow enough.

Noise model

Specifications:

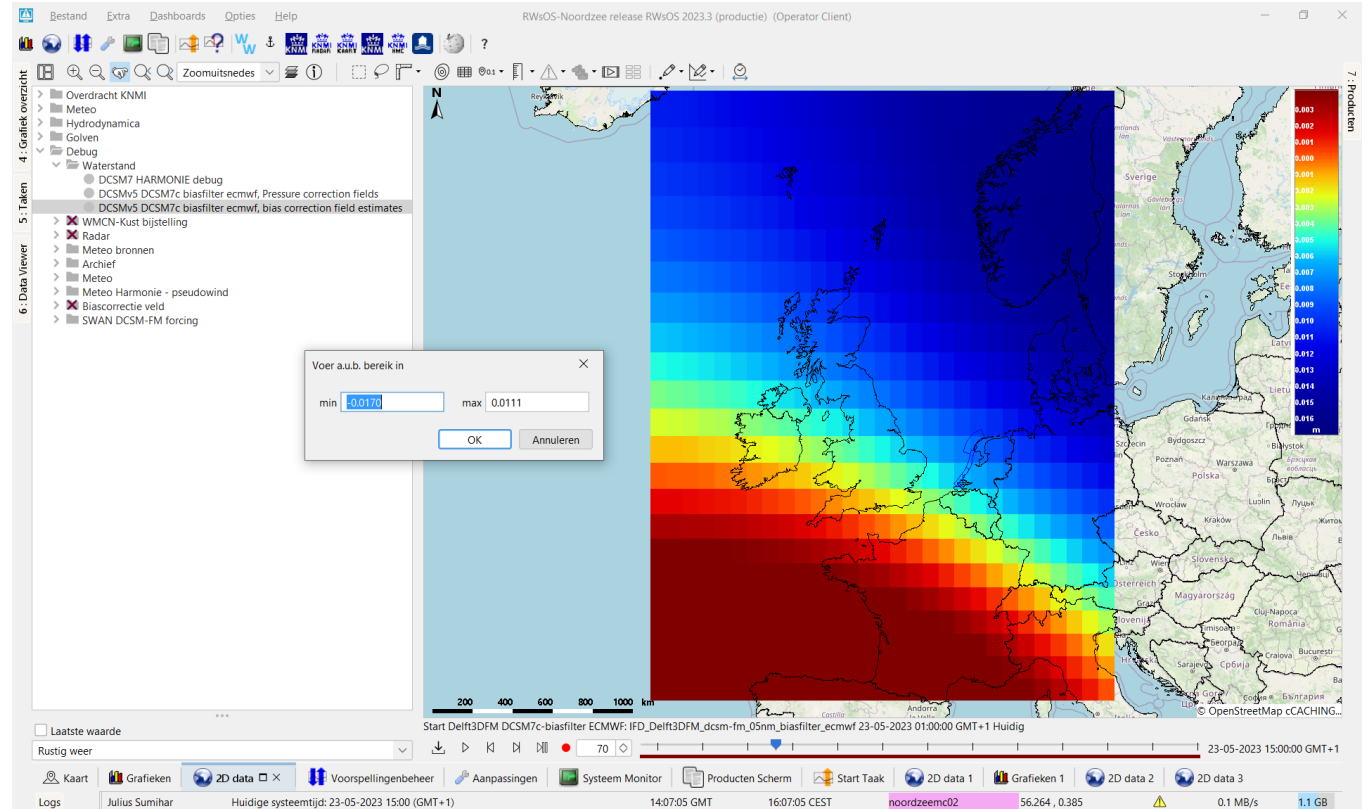
First-order autoregressive AR(1)

$$h_{bias,k+1}(x,y) = \alpha h_{bias,k}(x,y) + w_k(x,y)$$

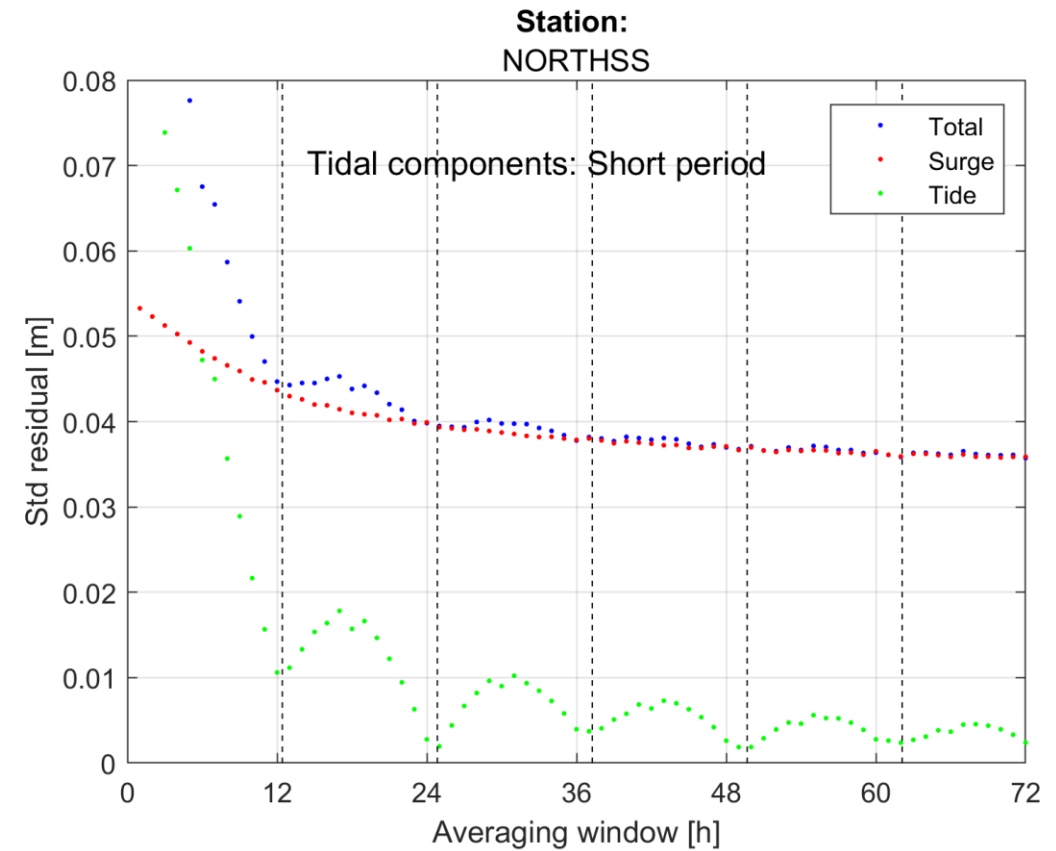
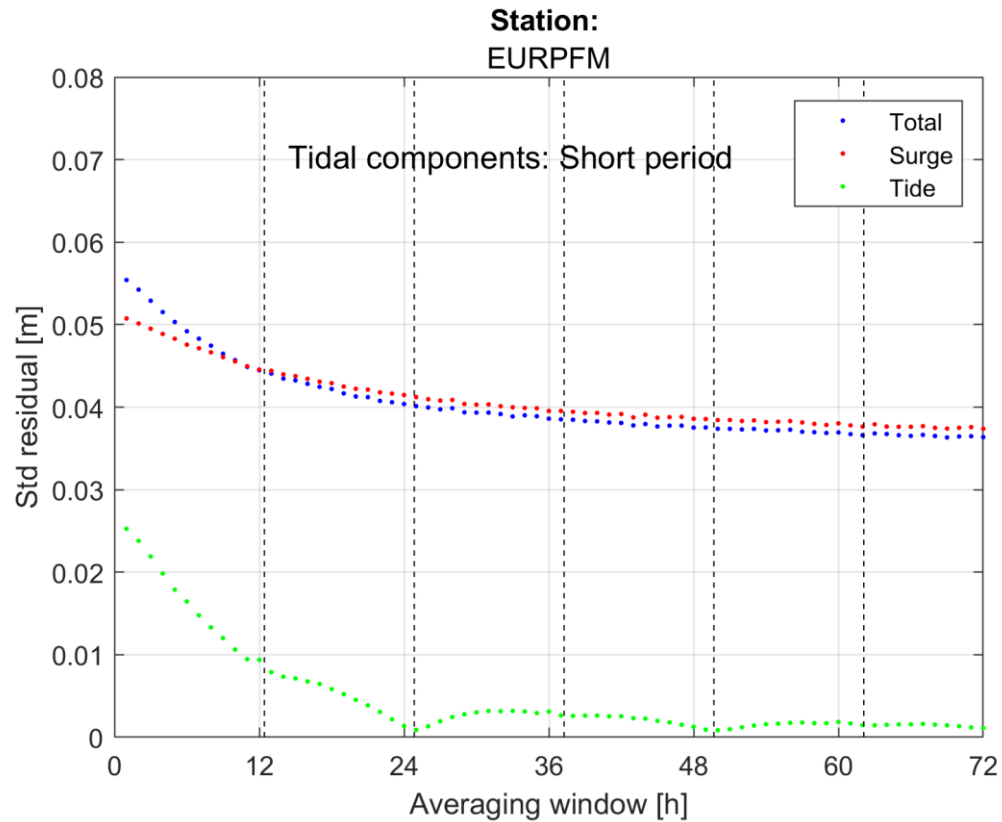
Time correlation scale: 750 hours

Horizontal correlation scale: 1500 km

$$w_k \sim N(0, Q)$$



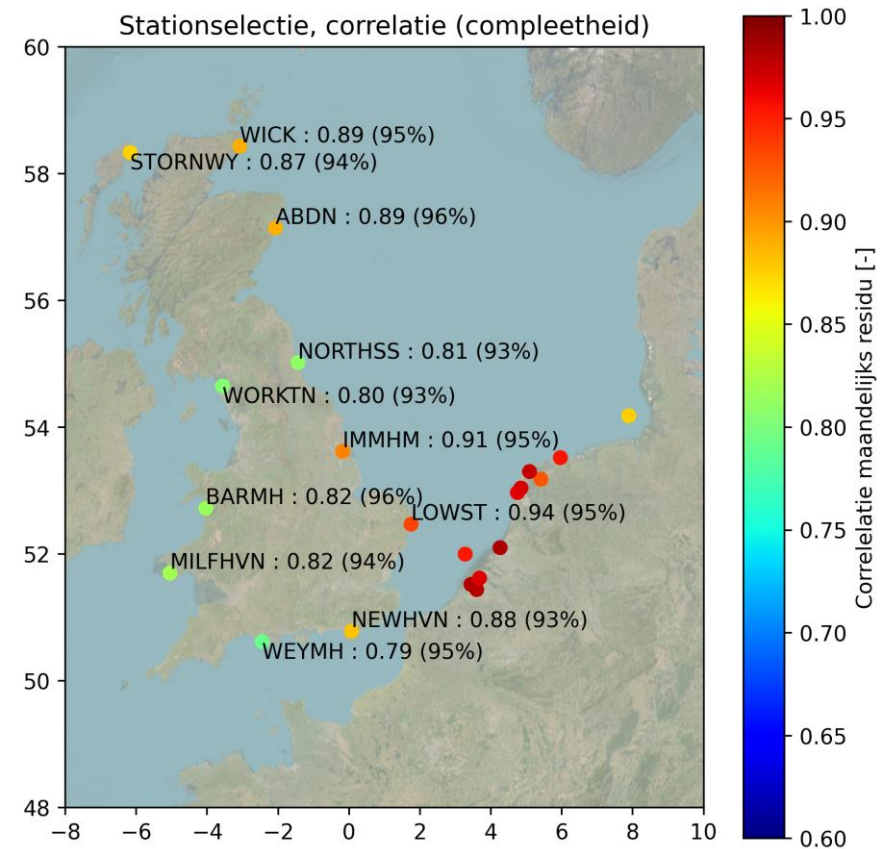
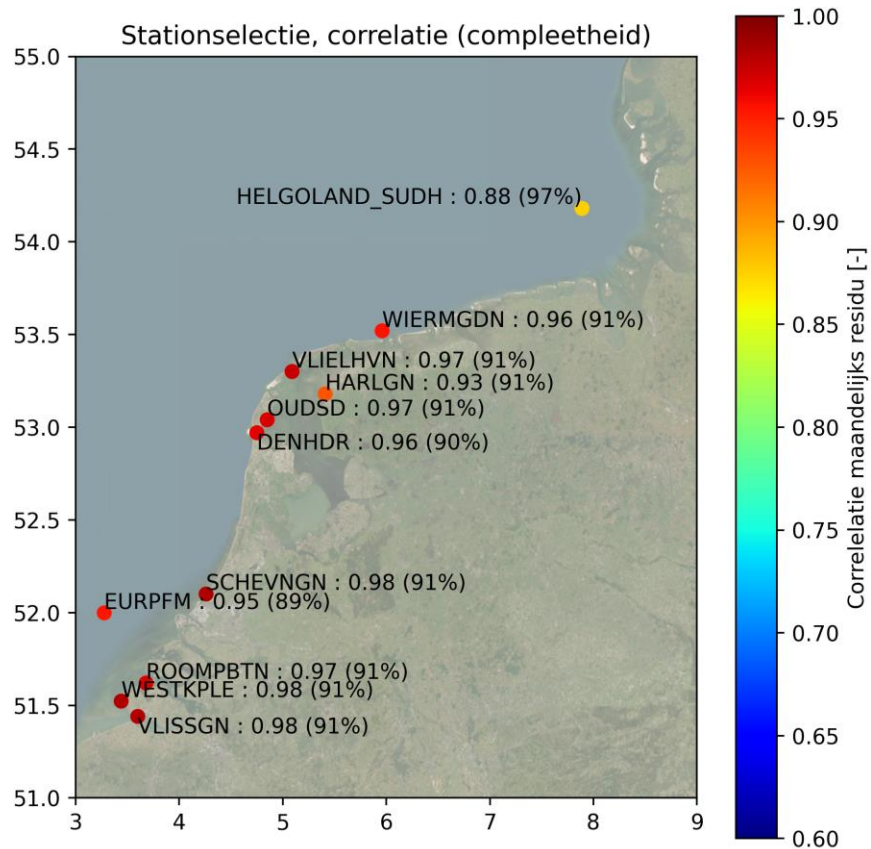
Temporal averaging of measurements



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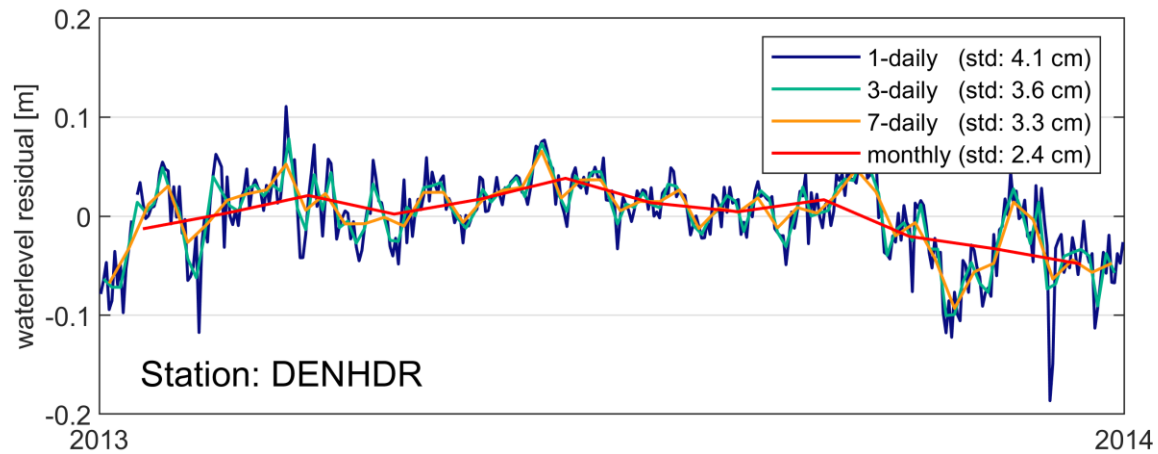
↑ 24hour average eliminates most tidal errors

The bias kalman filter assimilates daily waterlevels at 22 stations in the North Sea

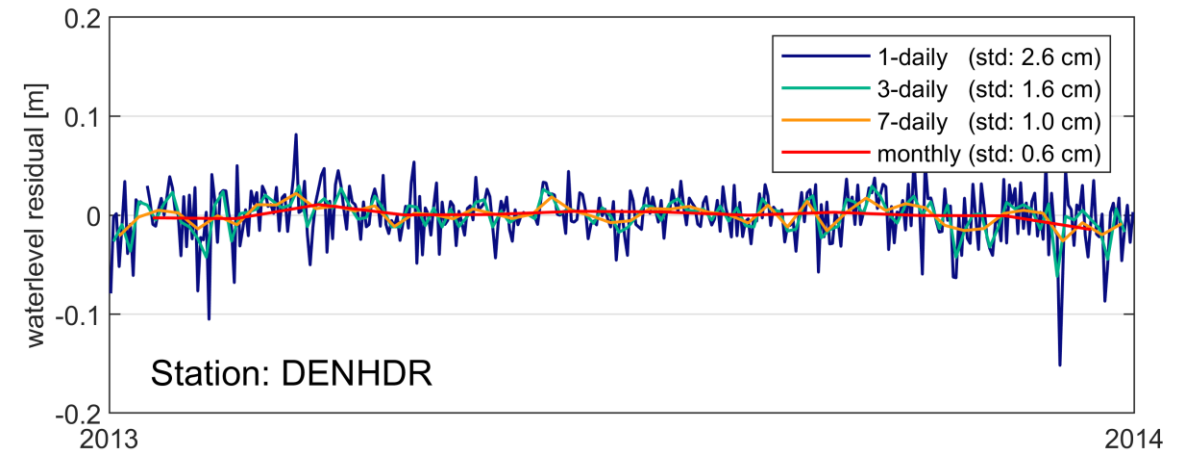


First results: example time-series of residuals from a hindcast

Simulation 2013 without bias Kalman filter

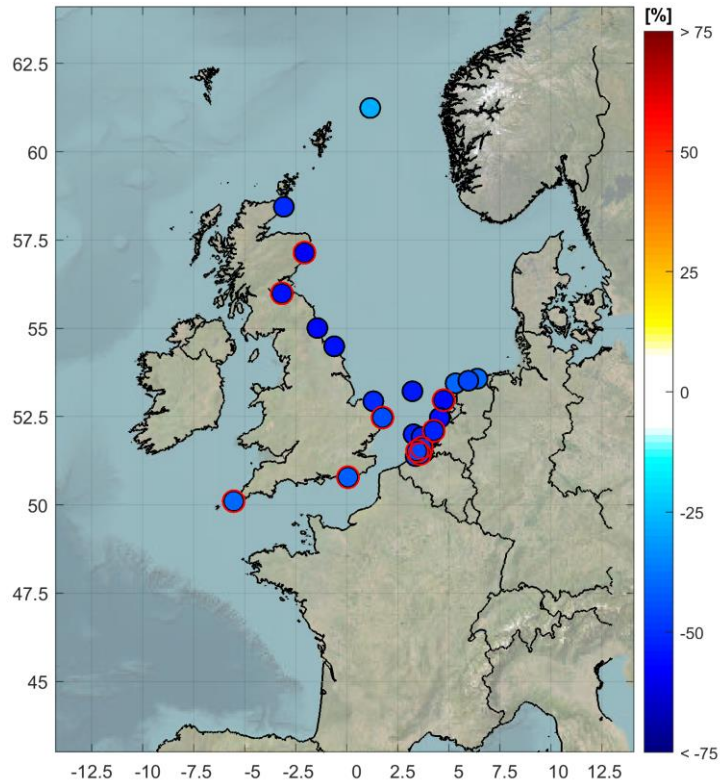


Simulation 2013 with bias Kalman filter

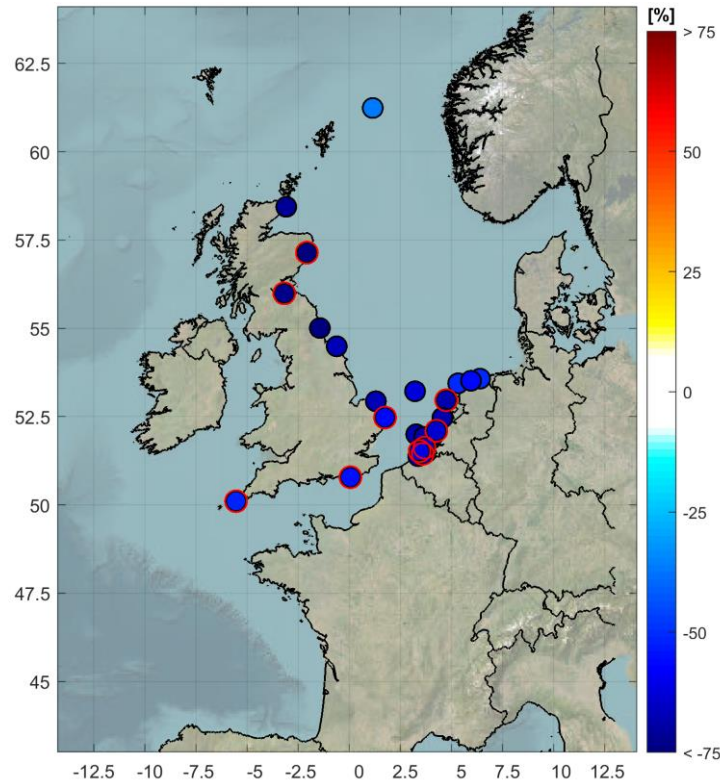


Impact on low-frequency residuals

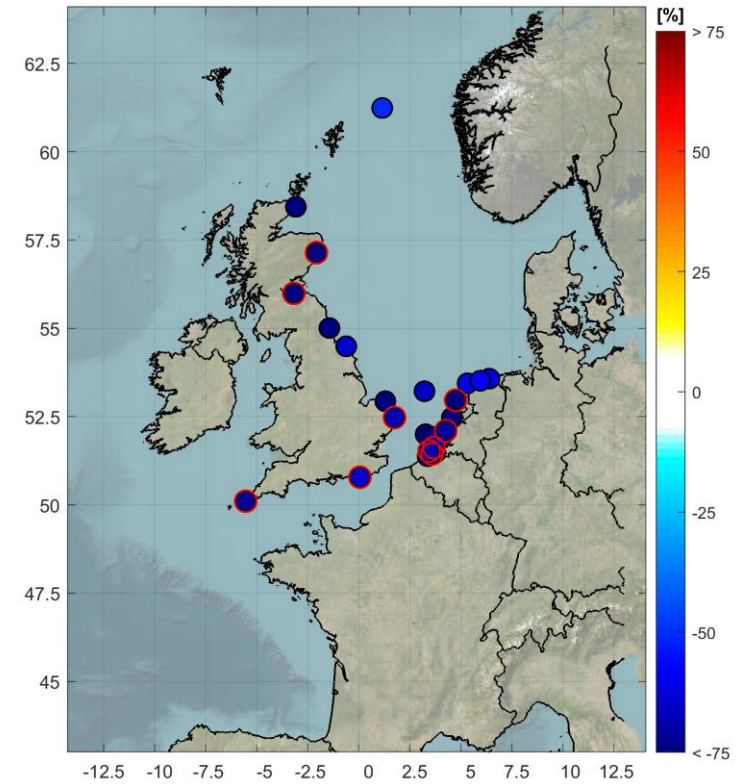
Change in std 3-day averaged residual rel. to reference simulation [%]



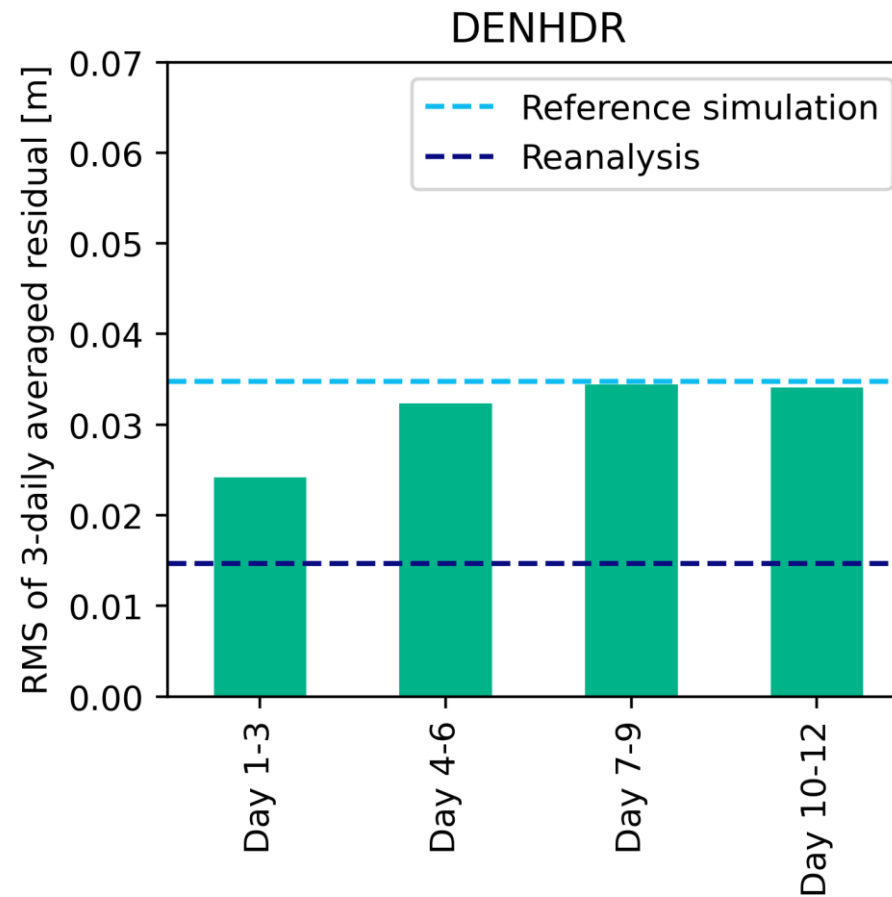
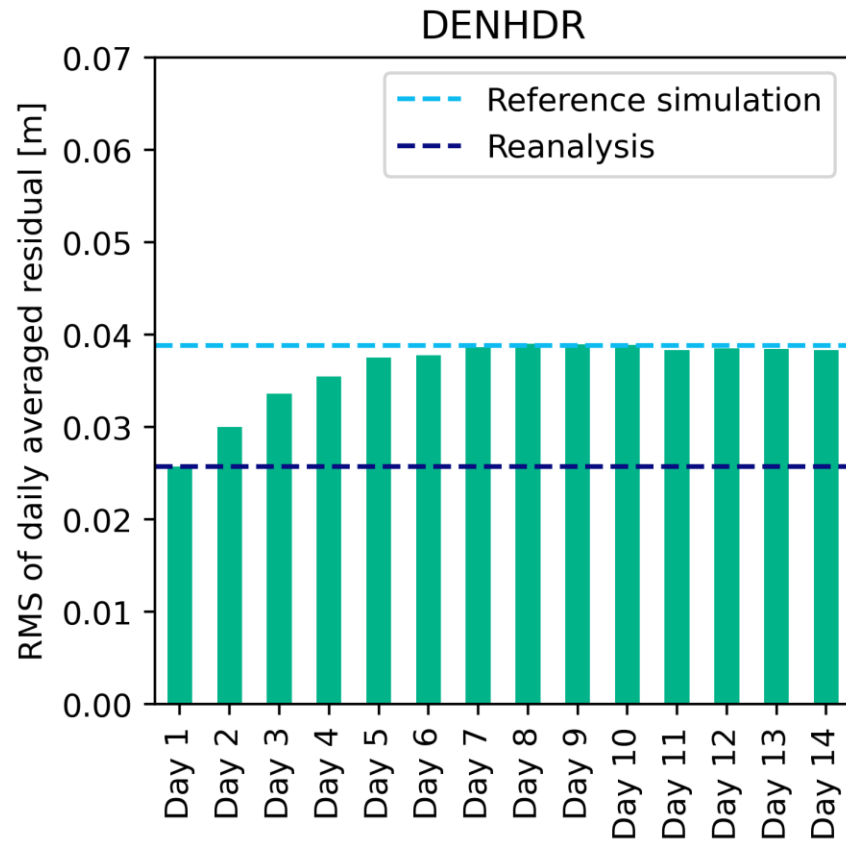
Change in std 7-day averaged residual rel. to reference simulation [%]



Change in std monthly residual rel. to reference simulation [%]



Forecast experiment with DCSM7 coarse



Reference simulation: Modelsimulation without biasKF
Reanalysis: Modelsimulation with daily assimilation of waterlevel residual

Steady state filter vs. Ensemble Kalman Filter

EnKF

Time update

$$\begin{aligned}\xi_{k+1}^f(i) &= \mathbf{M}(\xi_k^a(i)) \\ \hat{\mathbf{x}}_k^f &= \frac{1}{N} \sum_{i=1}^N \xi_k(i) \\ \mathbf{P}_k^f &= \frac{1}{N-1} \sum_{i=1}^N (\xi_k^f(i) - \hat{\mathbf{x}}_k^f)(\xi_k^f(i) - \hat{\mathbf{x}}_k^f)'\end{aligned}$$

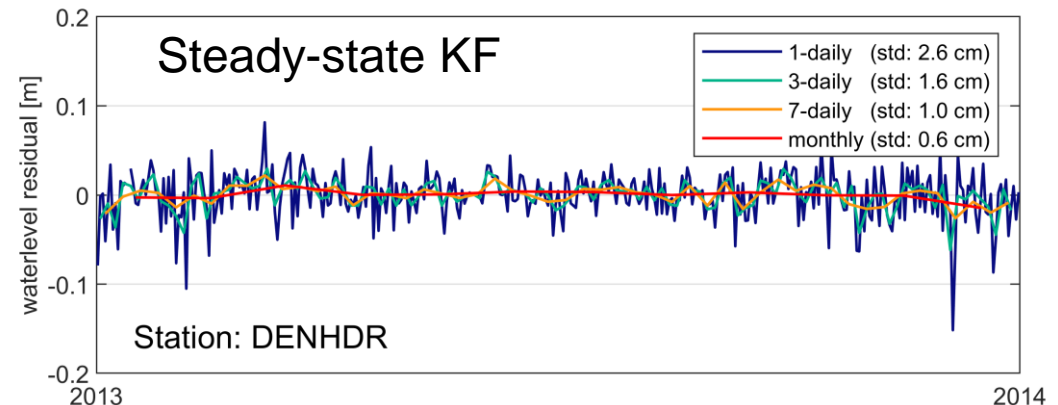
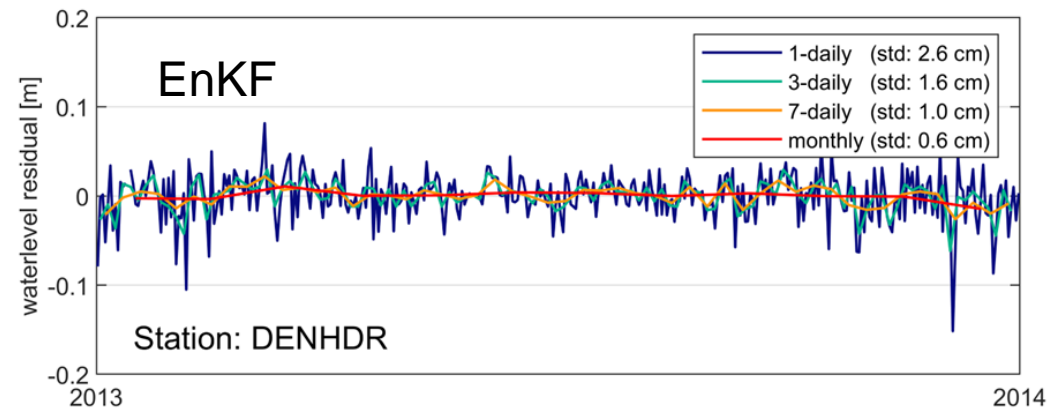
Measurement update

$$\mathbf{K}_k = \mathbf{P}_k^f \mathbf{H}' [\mathbf{H} \mathbf{P}_k^f \mathbf{H}' + \mathbf{R}]^{-1}$$

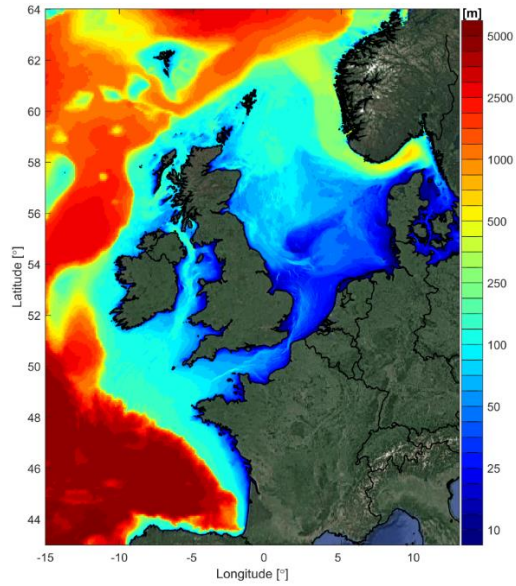
$$\xi_k^a(i) = \xi_k^f(i) + \mathbf{K}_k (z_k - \mathbf{H} \xi_k^f(i) - \mathbf{v}_k(i))$$

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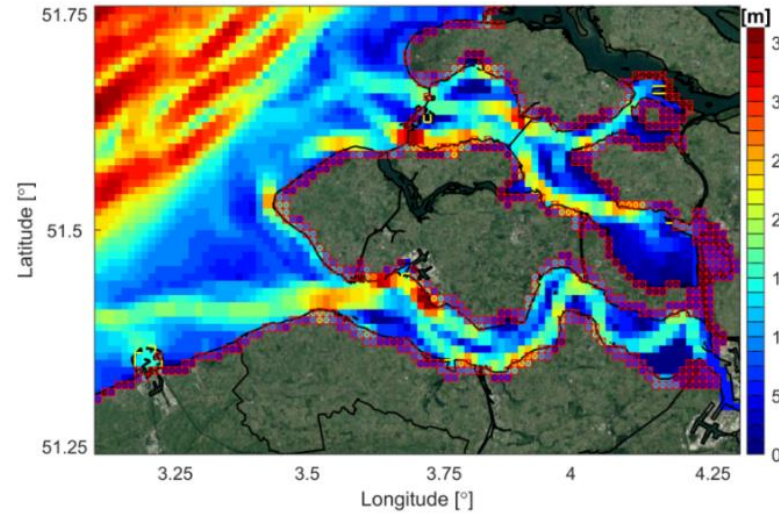
- If the Kalman Gain converges approximately to a steady value then steady-state filter is a much cheaper approximation



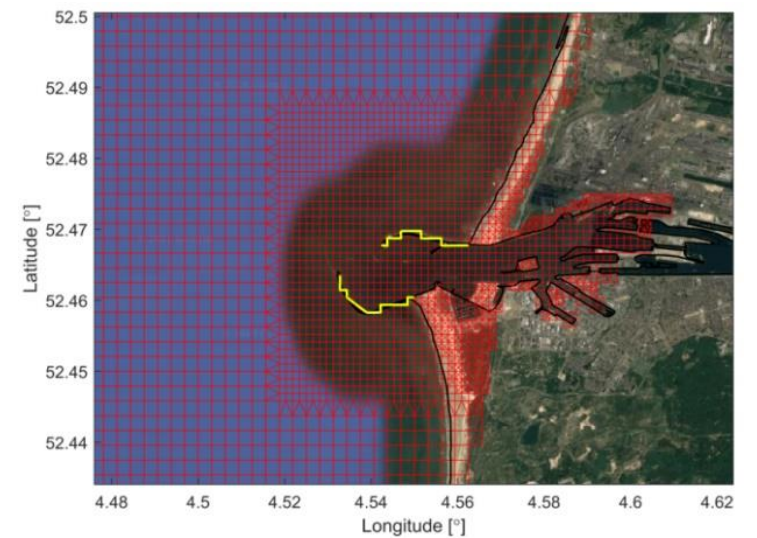
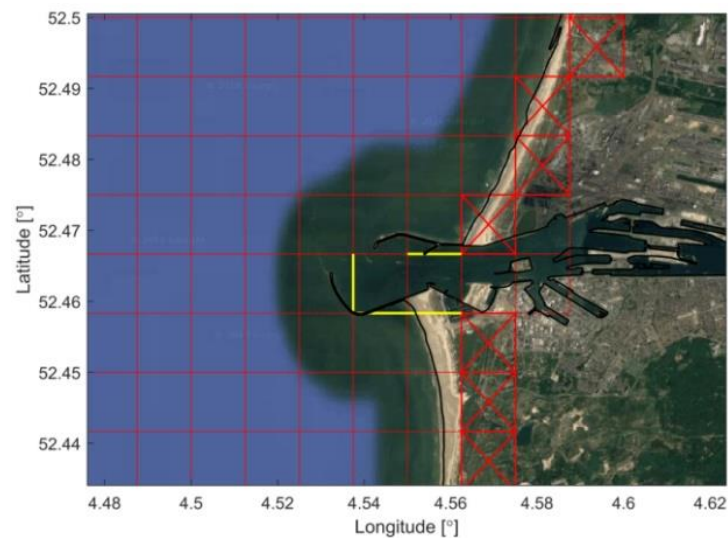
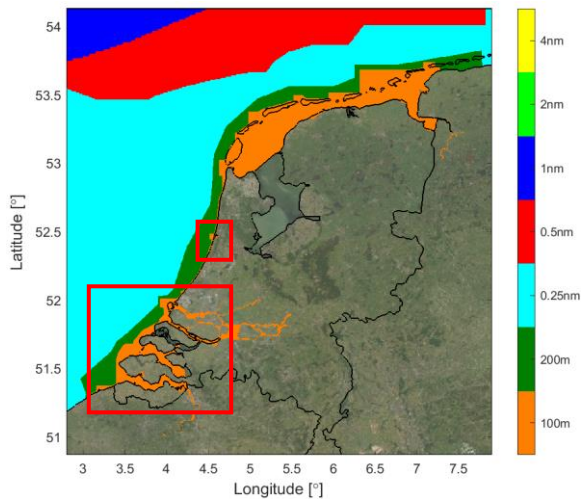
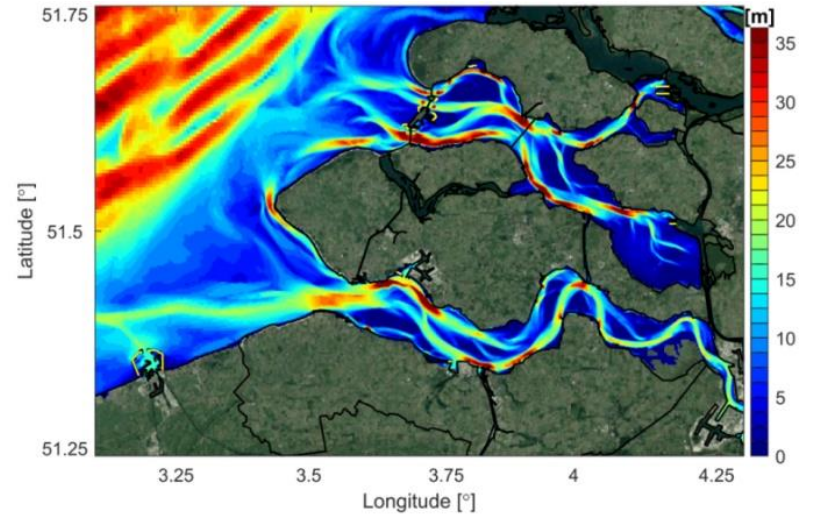
Apply estimated corrections to higher-resolution model



DCSM-FM 0.5 nm



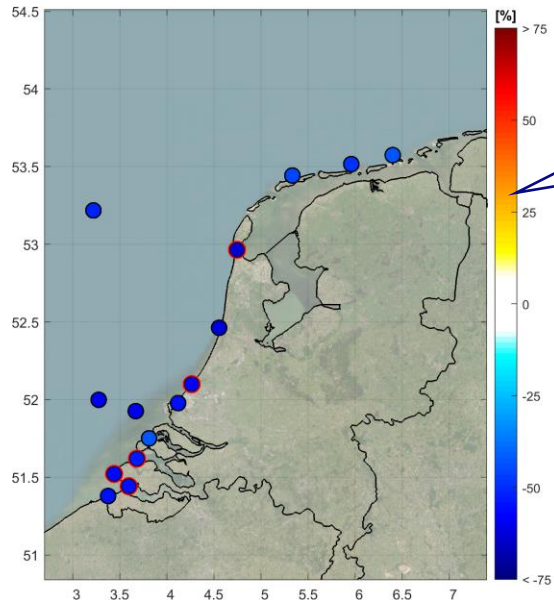
DCSM-FM 100m



'Bias correction field', applied to DCSM-FM 100m

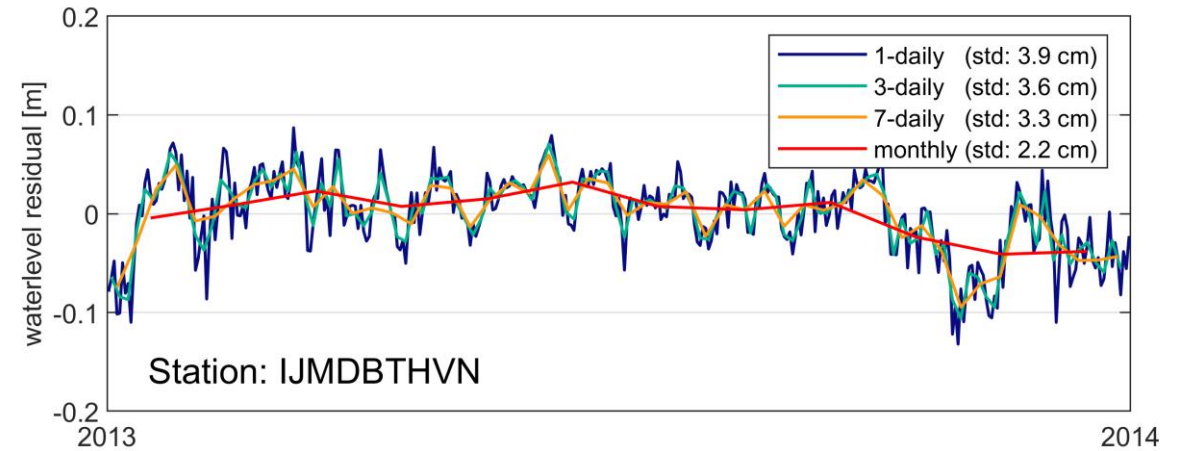
- Various model versions in operational system:
 - DCSM-FM 0.5nm
 - DCSM-FM 100m
- Estimate bias correction for coarse model and apply it to other models.

Change in std. 7-day averaged residual [%]

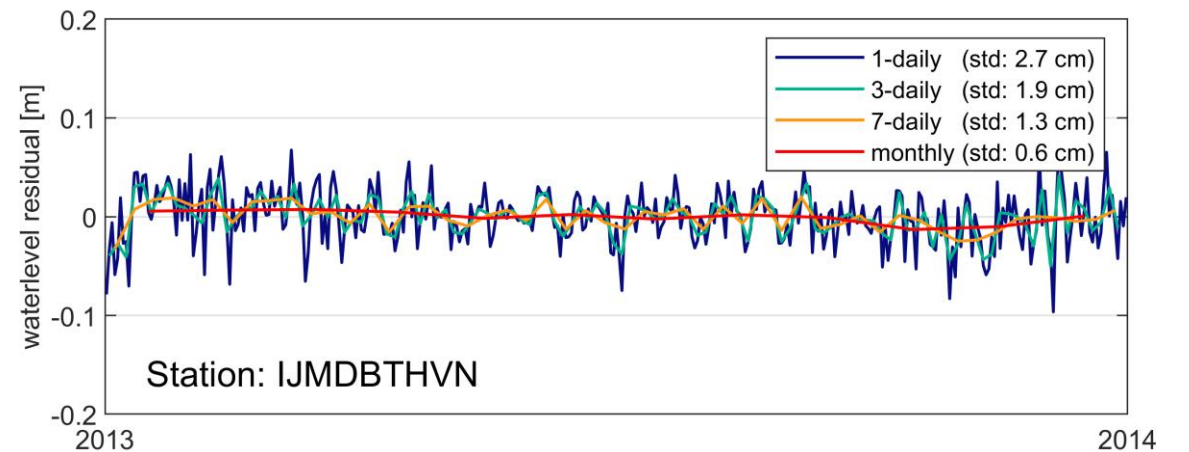


Average improvement: -56%

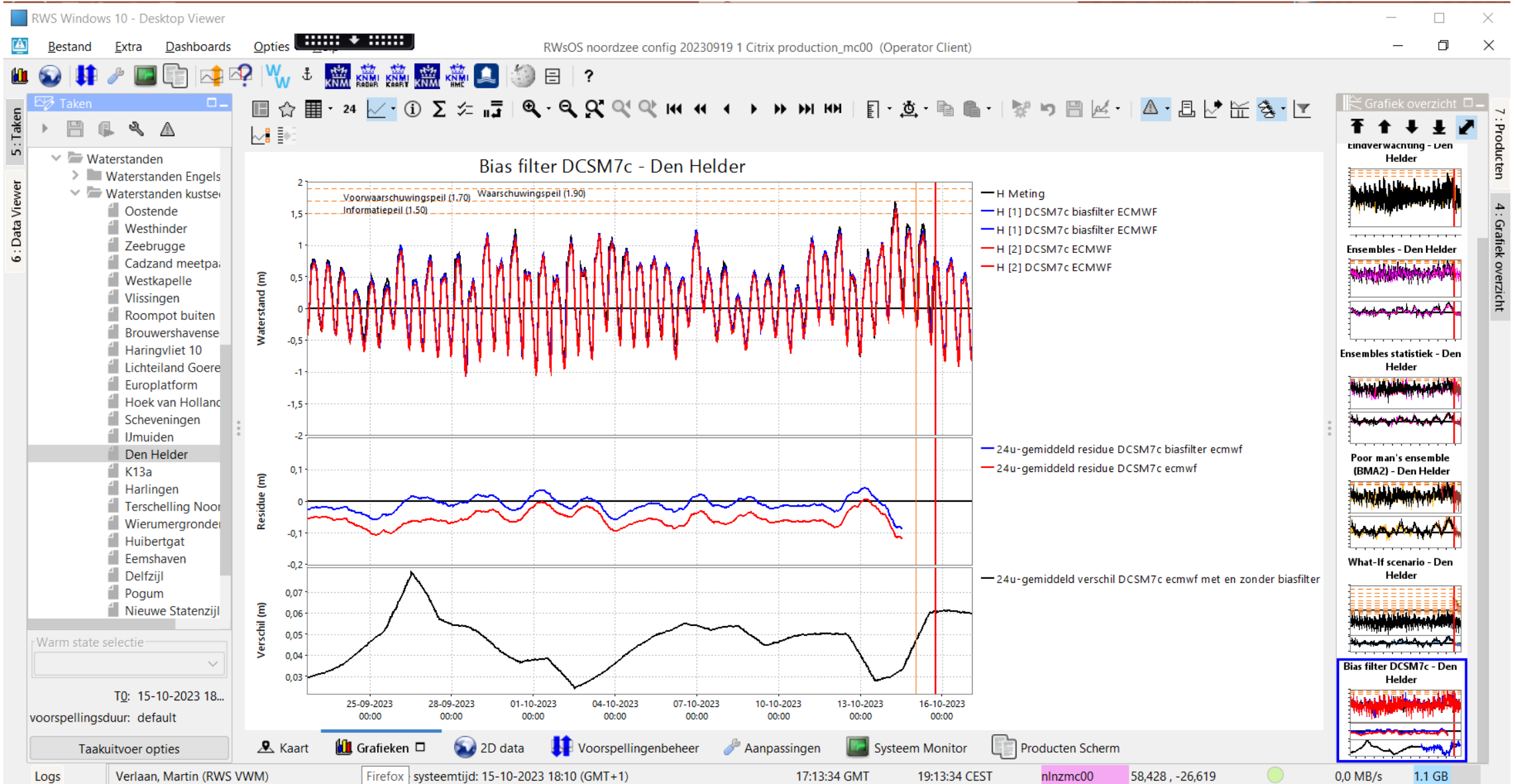
DCSM 100m without bias Kf



DCSM-FM 100m with bias correction derived from DCSM-FM 0.5nm

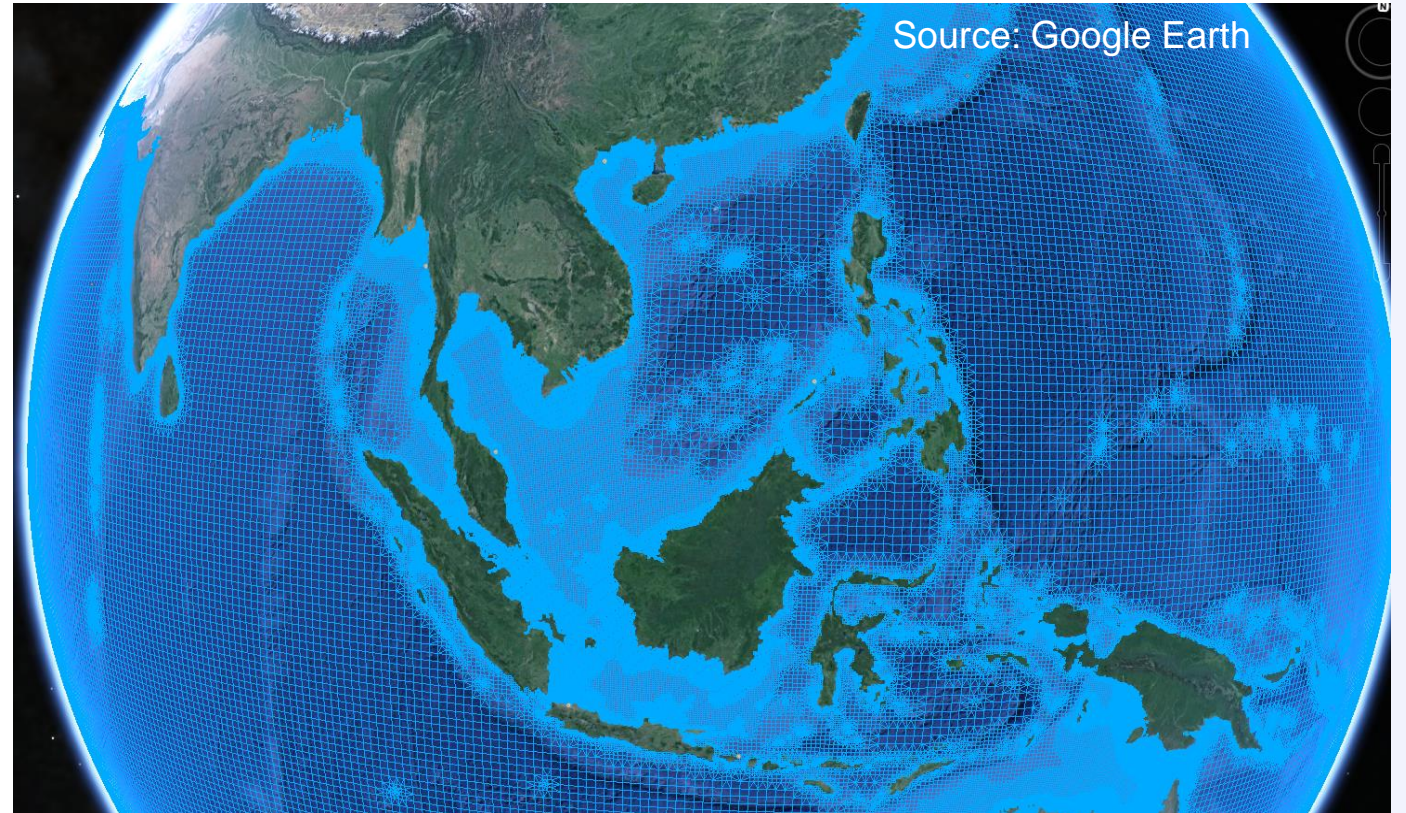


Pre-operational evaluation



Next steps

- Evaluation of pre-operational set-up for winter 2023-2024
- Connect downstream models
- Test use of satellite altimetry in global tide-surge model



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