On the sharp Hardy inequality in fractional Sobolev spaces

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We introduce the Hardy inequality on fractional Sobolev spaces $W^{s,p}(\Omega)$ and we look for the sharp constant on $\Omega \subset \mathbb{R}^N$ convex open set. Under the restriction $sp \geq 1$, our main tool is to construct supersolutions for the associated equation. Moreover, we observe that this method does not work for sp < 1, but we are able to overcome this limitation in the case p = 2. The results presented in this talk are obtained in collaboration with Francesca Bianchi (University of Parma), Lorenzo Brasco (University of Ferrara) and Firoj Sk (Okinawa Institute of Science and Technology).